

Single precision IEEE floating point (32 bits)

- First bit is the sign: 1 is negative, 0 is non-negative
- Next 8 bits represent the exponent in excess 127 notation (stored value is 127 larger than the exponent)
- Remaining 23 bits represent the fraction (mantissa), excluding the 1 to the left of the radix point
- Positive or negative infinity: exponent is all 1's and the fraction is 0
- Not-a-number (NaN): exponent is all 1's and fraction is anything non-zero

s - sign bit

f - fraction representation

e - exponent representation

$$1.f \times 2^{e-127}$$

negative if s is 1

Decimal

$$\begin{array}{ccccccc} & 0 & . & 1 & 3 & 5 & 2 & 6 \\ & & \nearrow & \uparrow & \uparrow & \nwarrow & & \\ \text{place} & \frac{1}{10} & & \frac{1}{100} & & \frac{1}{1000} & & \\ & 10^{-1} & & 10^{-2} & & 10^{-3} & & \dots \end{array}$$

Binary

$$\begin{array}{ccccccc} & 1 & . & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \\ & & \nearrow & \uparrow & \uparrow & \nwarrow & & & & & \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{8} & & & & & & & & \\ 2^{-1} & 2^{-2} & 2^{-3} & & & & & & & & \end{array}$$

- 62.125 to IEEE single-precision

$$62_{10} = 111110_2$$

$$0.125_{10} = 0.001_2$$

11110.001

shift radix point 5 places $\rightarrow 1.1110001_2 \times 2^{5_{10}}$

Exponent is 5, add 127 $\rightarrow$ 132

$$132_{10} = 10000100_2$$

Fraction, drop the 1 to the left of radix point, pad with zeros on the right

$$0 \times \frac{1100}{C} \frac{00100}{2} \frac{111}{7} \frac{1000}{8} \frac{1000}{8} \frac{00000}{0} \frac{00000}{0} \frac{00000}{0}$$

0.1

$$2^{-4} + 2^{-5} + 2^{-8} + 2^{-9} + 2^{-12} + 2^{-13} + \dots$$

(0.0625)

0.0001100110011001100 ...

Exponent is -4, add 127 $\rightarrow$ 123

1111011

Fraction

10011001100110011001100