## **CSCI 200**

## HW #2: Basic data structures and hashtables

**Directions:** Complete your work on a separate sheet of paper. Submit the physical copy of your work at the beginning of class on the specified due date. Show your work. You may work in groups of up to 3 students provided that all students participate in each question. Provide a short preliminary explanation of how an algorithm works before running an algorithm or presenting a formal algorithm description, and use examples or diagrams if they are needed to make your presentation clear.

- (a) You are given an initially empty stack S stored in array S[1...10]. Perform the following operations on it: PUSH(S, 'B'), PUSH(S, 'A'), PUSH(S, 'T'), PUSH(S, 'I'), POP(S), POP(S), PUSH(S, 'Z'), PUSH(S, 'A'), POP(S), PUSH(S, 'I'), PUSH(S, 'N'), PUSH(S, 'L'), POP(S), PUSH(S, 'G'), PUSH(S, 'A'), PUSH(S, 'R'), PUSH(S, 'F'), POP(S), POP(S). Show the contents of the stack after all operations have been performed, using figure 10.1 as a model, and indicate where the top of the stack is.
  - (b) You are given an initially empty queue Q stored in array Q[1...10]. Perform the following operations on it: ENQUEUE(Q, 'B'), ENQUEUE(Q, 'A'), ENQUEUE(Q, 'T'), ENQUEUE(Q, 'I'), DEQUEUE(Q), DEQUEUE(Q), ENQUEUE(Q, 'Z'), ENQUEUE(Q, 'A'), DEQUEUE(Q), ENQUEUE(Q, 'I'), ENQUEUE(Q, 'N'), ENQUEUE(Q, 'L'), DEQUEUE(Q), ENQUEUE(Q, 'G'), ENQUEUE(Q, 'A'), ENQUEUE(Q, 'R'), ENQUEUE(Q, 'F'), DEQUEUE(Q), DEQUEUE(Q). Show the contents of the queue after all operations have been performed, using figure 10.2 as a model, and indicate where the head and tail of the queue are.
- 2. Explain how to implement two stacks in one array A[1...n] in such a way that neither stack overflows unless the total number of elements in both stacks together is n. The PUSH and POP operations for both stacks should run in O(1) time.
- 3. Give the **pseudocode** for a linear-time algorithm for reversing a queue Q. To access the queue, you are only allowed to use the methods of a queue abstract data type (ENQUEUE, DEQUEUE, QUEUE-EMPTY). *Hint: You may use an auxiliary data structure.*
- 4. Explain how to implement a queue using two stacks. Analyze the running time of the queue operations.
- 5. Explain how to implement a stack using two queues. Analyze the running time of the stack operations.
- 6. Explain how to implement a queue using a singly linked list L. The operations ENQUEUE and DEQUEUE should still take O(1) time.
- 7. Give the **pseudocode** for a  $\Theta(n)$ -time non-recursive algorithm that reverses a singly linked list of n elements. The algorithm should run in-place, that is, it should use no more than constant storage beyond that needed for the list itself.
- 8. Draw a single binary tree T such that all of the following properties hold for T:
  - each node of T stores a single character,
  - a preorder traversal of T yields COMPILE, and
  - an inorder traversal of T yields PMIOLCE
- 9. Give the **pseudocode** for an algorithm called COMPUTEDEPTH(T) which runs in total O(n)-time and computes the depth of every node of a tree T, where n is the number of nodes of T. Assume every node has an attribute **depth** which has an initially null value, i.e., the purpose of the COMPUTEDEPTH algorithm is to appropriately set the depth attribute of every node with its correct depth value. *Hint: After you have set a particular node's depth attribute, you may access it later to help set another node's depth attribute.*
- 10. Use the table below to convert a character key to an integer. For each of the following questions, give the contents of the hash table that results when the following keys are inserted into an initially empty 13-item hash table, which has indices 0 to 12. The keys to insert, in this order, are:  $(E_1, A, S_1, Y, Q, U, E_2, S_2, T, I, O, N)$ . Use  $h(k) = k \mod 13$  for the hash function for the k-th letter of the alphabet (see above table for converting letter keys to integer values). Use the provided method to resolve collisions. Note that the elements to insert into the hashtable are letters. not numbers.

Letter	Α	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М
Key	0	1	2	3	4	5	6	7	8	9	10	11	12
Letter	Ν	0	Р	Q	R	S	Т	U	V	W	Х	Υ	Z
Key	13	14	15	16	17	18	19	20	21	22	23	24	25

- (a) Illustrate the contents of the hashtable when collisions are resolved using chaining.
- (b) Illustrate the contents of the hashtable when collisions are resolved using **linear probing**.
- (c) Illustrate the contents of the hashtable when collisions are resolved using **double hashing**. Let the secondary hash function be  $h'(k) = 1 + (k \mod 11)$ .